

Blood Shear Stress Calculation

$$(1) \tau = \eta\gamma$$

$$(2) \gamma = \frac{8v}{d}$$

$$(3) v = \frac{l}{t}$$

$$(4) \tau = \eta \frac{8l}{dt}$$

τ = wall shear stress
 η = viscosity (blood = 3.5 cP)
 γ = shear rate
 v = mean velocity
 d = diameter
 l = length
 t = time

Assume 100 mm collateral arterial length and 0.7 mm collateral arterial diameter. Also assume 0.03 second calf muscle contraction during normal walking, and a 0.25 second pressure application time for the ArtAssist (model AA-100)

Using equation (4):

$$\text{Shear stress from walking: } \tau = (0.035p) \frac{8 \frac{100\text{mm}}{0.3\text{s}}}{0.7\text{mm}} = \mathbf{133\text{ Pa}} = \mathbf{1330\text{ dyn/cm}^2}$$

$$\text{Shear stress from the ArtAssist machine: } \tau = (0.035p) \frac{8 \frac{100\text{mm}}{0.25\text{s}}}{0.7\text{mm}} = \mathbf{160\text{ Pa}} = \mathbf{1600\text{ dyn/cm}^2}$$

Pressure/time ratios

Using a normal walking speed of 100 steps/min = 1.6 steps/sec
 = 0.83 steps/sec (for one leg) = 1.2 seconds/step

Muscle contracts for about a fourth of time of the gait cycle¹

Each muscle contraction lasts \approx 0.3 seconds

Applied pressures:

Soleus = 250 mmHg² = 33,330 Pa

Gastrocnemius = 215 mmHg² = 28,664 Pa

Machine = 120 mmHg = 15,998 Pa

$$\text{Soleus} = \frac{33,330\text{ Pa}}{0.3\text{ s}} = \mathbf{111,100\text{ Pa/sec}}$$

$$\text{Gastrocnemius} = \frac{28,664\text{ Pa}}{0.3\text{ s}} = \mathbf{95,546\text{ Pa/sec}}$$

$$\text{ArtAssist Machine} = \frac{15,998\text{ Pa}}{0.25\text{ s}} = \mathbf{63,992\text{ Pa/sec}}$$

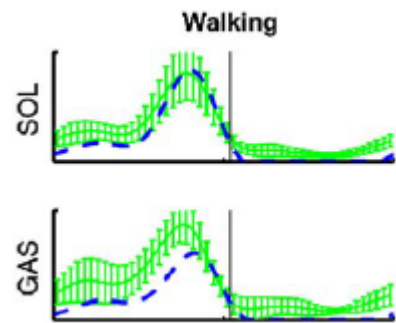


Figure 1: Muscle excitation patterns for walking¹

¹ Sasaki, Koraro and Neptune, Richard R. 2006. "Differences in Muscle Function during walking and running at the Same Speed" *Journal of Biomechanics*. 39

² "Strandness, Eugene D. and Sumner, David S., 1975, *Hemodynamics for Surgeons*. New York, NY, 137 p.